

Tribhuvan University  
Institute of Science and Technology

2080



Bachelor Level / First Year/ Second Semester/ Science  
**Computer Science and Information Technology (CSC160)**  
(Discrete Structure)  
**(OLD COURSE)**

Full Marks: 60  
Pass Marks: 24  
Time: 3 hours.

*Candidates are required to give their answers in their own words as far as practicable.*  
The figures in the margin indicate full marks.

**Section A**

**Long answer questions.**

**Attempt any TWO questions.**

(2×10=20)

1. Explain proof by contraposition and proof by contradiction. Show that if  $n$  is an integer and  $n^3 + 5$  is odd, then  $n$  is even using a) a proof by contraposition, b) a proof by contradiction.  
(4 + 3 + 3)
2. Define recurrence relation. Compare linear homogeneous recurrence relation with linear nonhomogeneous recurrence relation. What is the solution of the recurrence relation  $a_n = -4a_{n-1} - 4a_{n-2}$  for  $n \geq 2$ ,  $a_0 = 0$ ,  $a_1 = 1$ ?  
(2 + 2 + 6)
3. Explain graph as models of flow of Commodities. How do you find maximal flow in the transport network? State max-flow min-cut theorem.  
(2 + 6 + 2)

**Section B**

**Short answer questions.**

**Attempt any EIGHT questions.**

(8×5=40)

4. How can you represent sets using bit strings? Let  $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ . What bit strings represent the subset of all odd integers in  $U$ , the subset of all even integers in  $U$ , and the subset of integers not exceeding 5 in  $U$ ?  
(2 + 3)
5. Define floor and ceiling function. What do you mean by exponential function?  
(3 + 2)
6. Define summation. What is the value of the double sum  $\sum_{i=1}^2 \sum_{j=1}^3 (i + j)$ ?  
(1 + 4)
7. Explain Euclidean algorithm. Use this algorithm to find  $\gcd(111, 201)$ .  
(2 + 3)
8. Find the Boolean product of  $A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}$ .  
(5)
9. Define predicate. Compare existential quantifier with universal quantifier.  
(1 + 4)
10. What is structural induction? Explain.  
(5)
11. What is the probability that a positive integer selected at random from the set of positive integers not exceeding 100 is divisible by either 2 or 5?  
(5)
12. Explain Hamilton path and circuit with suitable example.  
(2.5 + 2.5)